A R T I C L E S
Published on Web 04/19/2006

# Computational Study of Carbon Atom ( ${ }^{3} \mathrm{P}$ and ${ }^{1} \mathrm{D}$ ) Reaction with $\mathrm{CH}_{2} \mathrm{O}$. Theoretical Evaluation of ${ }^{1} \mathrm{~B}_{1}$ Methylene Production by C ( ${ }^{1} \mathrm{D}$ ) 

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#### Abstract

Singlet and triplet free energy surfaces for the reactions of C atom ( ${ }^{3} \mathrm{P}$ and ${ }^{1} \mathrm{D}$ ) with $\mathrm{CH}_{2} \mathrm{O}$ are studied computationally to evaluate the excited singlet $\left({ }^{1} B_{1}\right)$ methylene formation from deoxygenation of $\mathrm{CH}_{2} \mathrm{O}$ by $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ atom as suggested by Shevlin et al. Carbon atoms can react by addition to the oxygen lone pair or to the $\mathrm{C}=\mathrm{O}$ double bond on both the triplet and singlet surfaces. Triplet $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ atoms will deoxygenate to give CO plus $\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ as the major products, while singlet $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ reactions will form ketene and CO plus $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$. No definitive evidence of the formation of excited singlet $\left({ }^{1} \mathrm{~B}_{1}\right)$ methylene was found on the singlet free energy surface. A conical intersection between the ${ }^{1} \mathrm{~A}^{\prime}$ and ${ }^{1} \mathrm{~A}^{\prime \prime}$ surfaces located near an exit channel may play a role in product formation. The suggested ${ }^{1} \mathrm{~B}_{1}$ state of methylene may form via the ${ }^{1} A$ " surface only if dynamic effects are important. In an effort to interpret experimental observation of products trapped by (Z)-2-butene, formation of cis- and trans-1,2-dimethylcyclopropane is studied computationally. The results suggests that "hot" ketene may react with (Z)-2-butene nonstereospecifically.


## Introduction

The chemistry of atomic carbon is central to the mechanistic and quantitative understanding of organic chemistry in that it is the ultimate case of a low-valent carbon-centered reactive intermediate that exhibits a thermodynamic drive to form a tetravalent carbon. However, it is very difficult to achieve a complete understanding of C atom reactions because the reaction of C atom produces other reactive intermediates, such as carbenes, which can react to form more stable products. Hence, the experimental studies of the mechanisms of C atom reactions have often been limited, and complementary computational studies have been utilized successfully. ${ }^{1}$

Most reactions of C atoms are highly exothermic because of the extremely high heat of formation of the C atom. The groundstate atomic carbon is triplet $\left({ }^{3} \mathrm{P}\right)$, with a heat of formation ( $\Delta H_{\mathrm{f}}{ }^{\circ}$ ) of $171 \mathrm{kcal} / \mathrm{mol}$. The first and second excited states are singlet states, ${ }^{1} \mathrm{D}$ with $\Delta H_{\mathrm{f}}{ }^{\circ}=201 \mathrm{kcal} / \mathrm{mol}$ and ${ }^{1} \mathrm{~S}$ with $\Delta H_{\mathrm{f}}{ }^{\circ}$ $=233 \mathrm{kcal} / \mathrm{mol}$, respectively. ${ }^{1,2}$ Many of the C atom reactions involve the ${ }^{1} \mathrm{D}$ state, and this species brings an additional 30 $\mathrm{kcal} / \mathrm{mol}$ of energy to its reaction. Therefore, the products from C atom reactions contain a great deal of excess energy. When the initial product of a C atom reaction is another reactive intermediate such as a carbene, then very interesting reactivity can be observed due to the high exothermicity. ${ }^{1,3}$

When C atoms react with unsaturated hydrocarbons, abstraction of hydrogen, insertion into a $\mathrm{C}-\mathrm{H}$ bond, or $\pi$ addition
(1) Shevlin, P. B. In Reactive Intermediate Chemistry; Moss, R. A., Platz, M. S., Jones, M., Jr., Eds.; Wiley: New York, 2004; p 463.
(2) Chase, M. W., Jr. NIST-JANAF Thermochemical Tables, 4th ed.; J. Phys Chem. Ref. Data Monograph 9; American Institute of Physics: Washington, DC, 1998.
occurs. ${ }^{1,4-8}$ In analogy with carbenes, ${ }^{9}$ atomic carbon reacts with alkenes by double-bond addition to give cyclopropylidenes which undergo ring-opening to allenes. In the case of carbonyl compounds, the ${ }^{1} \mathrm{D} C$ atom can react in a similar fashion: carbon atom addition to the $\mathrm{C}=\mathrm{O}$ double bond followed by ringopening to give a ketene, as shown in eq 1 . There is also the

possibility of end-on attack via a lone pair of electrons on oxygen, forming an ylide-like species $\left(\mathrm{R}_{2} \mathrm{C}-\mathrm{O}-\mathrm{C}\right)$. However, no compelling evidence for the end-on intermediate has been reported. ${ }^{10}$ Although a ketene is the global minimum on the

[^0]potential energy surfaces, no ketene has been isolated. While the existence of an intermediate ketene was confirmed by the formation of pentanoic acid by the reaction with $\mathrm{H}_{2} \mathrm{O}$ in the process of the reaction of arc-generated carbon with butanal, ${ }^{10}$ the major products of the reaction of arc-generated carbon with carbonyl compounds come from carbenes which are formed from deoxygenation of the carbonyl compounds. Although $\mathrm{C}=$ C double bond cleavage in ketene is highly endothermic, this reaction is still feasible because of the high exothermicity of the initial reaction.

It is well established that deoxygenation occurs in the reaction of $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ atoms with ketones and aldehydes. ${ }^{1,10-16}$ Furthermore, it has been suggested that singlet excited-state $\left({ }^{1} \mathrm{~B}_{1}\right)$ carbenes form in the $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ atom deoxygenation of formaldehyde ${ }^{13}$ and cyclopentanone. ${ }^{16}$ The C atom deoxygenation of formaldehyde was reported in 1983 by Shevlin, where the generated carbene was allowed to react with ( $Z$ )-2-butene. After assessing the stereochemistry of the product mixture, the formation of $\mathrm{CH}_{2}$ $\left({ }^{1} B_{1}\right)$ was suggested. ${ }^{13}$ However, the excited singlet carbene in this deoxygenation process was not observed, and it is still not clear how it can form.

Numerous studies of the $\mathrm{CH}_{2} \mathrm{CO}$ potential energy surface (PES) have been reported, ${ }^{17-23}$ including electronic states, photodissociation pathways, and oxirene rearrangements. However, a comprehensive studies of the PES for $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}$ is lacking. Hereupon, we report a computational study of C atom reactions in the ground state $\left({ }^{3} \mathrm{P}\right)$ and first excited state $\left({ }^{1} \mathrm{D}\right)$ with formaldehyde.

## Computational Details

The Gaussian03 program ${ }^{24}$ was used for the hybrid density functional PBE1PBE ${ }^{25}$ calculations, while the GAMESS program ${ }^{26}$ was used for Complete Active Space SCF (CASSCF) ${ }^{27}$ and MCQDPT2 ${ }^{28}$ calculations. Geometry optimizations for minima and transition states were carried out at the (U)PBE1PBE/6-311++G(3df,p) (DFT) and CASSCF$(14,13) / 6-311+\mathrm{G}(2 \mathrm{~d}, \mathrm{p})$ (CAS) levels. At the DFT level, harmonic

[^1]vibrational analysis was performed and the minima and transition states were characterized. Thermodynamic correction terms, zero-point vibrational energies (ZPC), heat capacity corrections, and entropies (at 298 K) were obtained at the DFT level. Transition vectors of transition states were visualized by the MOLDEN program, ${ }^{29}$ and if necessary, IRC calculations were carried out to connect the transition state to the corresponding minima.

For CASSCF geometry optimization, a $(14,13)$ active space (14 electrons in 13 orbitals) was chosen from the full $(16,14)$ valence active space of $\mathrm{CH}_{2} \mathrm{CO}$. To maintain a consistent active space, we included all valence electrons except for the oxygen lone pair that lies lowest in energy. For the product fragments, we considered the same orbitals so that the total active space was maintained as in $\mathrm{CH}_{2} \mathrm{CO}$. For example, a $(6,6)$ active space was used for $\mathrm{CH}_{2}$ and a $(8,7)$ active space was used for CO.

At each stationary point at the CAS level, single-point energy calculations were carried out at the MCQDPT2/6-311+G(2d,p) (MCPT) level. Since the $(14,13)$ active space calculations at the MCPT level are very challenging in terms of computing resources and computing cost, a $(12,11)$ active space was used, where one low-lying $\mathrm{C}-\mathrm{H}$ bonding orbital and its antibonding orbital were excluded. The active space of product fragments was chosen in the same way as at the CAS level $\left(a(4,4)\right.$ active space for $\mathrm{CH}_{2}$ and a $(8,7)$ active space for CO$)$. The potential energy surfaces were constructed at the MCPT level with zero-point energy correction, heat capacity correction, and free energy correction calculated at the DFT level. The singlet and triplet surfaces are considered separately, and possible singlet-triplet crossings are not considered in this study. Further wave function analysis was carried out with CASSCF wave functions to examine correlations between the reaction intermediates and the products. We will use a notation scheme with a boldface " $\mathbf{S}$ " for singlets and " $\mathbf{T}$ " for triplets followed by one number for minima and two numbers or one number and a character for transition states. Thus, S12 is the singlet transition state between $\mathbf{S 1}$ and $\mathbf{S} 2$ and T5p is the transition state between $\mathbf{T 5}$ and products. We have not used the same numbering system between singlets and triplets, i.e., $\mathbf{S 3}$ is a carbene while $\mathbf{T 3}$ is the oxirene. A computational study of the ketene plus ( $Z$ )-2-butene reaction was carried out at the PBE1PBE/6-311+G(2d,p) level in an effort to rationalize the observed trapped products.

## Result and Discussion

The structural isomers of $\mathrm{CH}_{2} \mathrm{CO}$ in the singlet and triplet states at the DFT and CAS level are given in Figures 1 and 2. The calculated electronic energies and thermodynamic correction terms and spin-squared values are listed in Table 1. Numerous theoretical calculations on electronic states and photodissociation paths of $\mathrm{CH}_{2} \mathrm{CO}$ have been reported. ${ }^{17-23}$ The obtained geometric parameters in this study are in good agreement with those available in the literature, ${ }^{17-23}$ which are not given in Figures 1 and 2 for reasons of clarity. The geometries of $\mathbf{S} 2\left({ }^{1} \mathrm{~A}_{1}\right), \mathbf{S} 4$ $\left({ }^{1} \mathrm{~A}_{1}\right)$, $\mathbf{T} 2\left({ }^{3} \mathrm{~A}^{\prime \prime}\right)$, and $\mathbf{T} 2 \mathbf{p}\left({ }^{3} \mathrm{~A}^{\prime \prime}\right)$ optimized at the DFT and CAS levels show good agreement with previous studies by East, ${ }^{19 b}$ Schaefer, ${ }^{18 \mathrm{~b}, 23 \mathrm{a}}$ and Nemes. ${ }^{19 \mathrm{c}}$ The $\mathbf{C}=\mathrm{C}$ bond of $\mathbf{S} \mathbf{2}$ is shorter than a normal double bond distance due to the electron

[^2]

Figure 1. Optimized geometries of singlet species at the DFT (PBE1PBE/6-311++G(3df,p)) and CAS (CAS (14,13)/6-311+G(2d,p)) (in italic) levels. Literature values (underlined) for $\mathbf{S} 2$ and $\mathbf{S} 4$ are from refs 19 b and 23a, respectively. The $\mathbf{S}_{\mathrm{ci}}$ (surface crossing) geometry was obtained at the CASSCF$(6,6) / 6-311+G(2 d, p)$ level. Bond lengths are in angstroms and angles are in degrees.
delocalization over the $\mathrm{C}-\mathrm{C}-\mathrm{O} \pi$ bonding system. On the triplet surface, $\mathbf{T} \mathbf{2}$ is the lowest-energy structure, with a normal $\mathrm{C}-\mathrm{C}$ single bond distance of $1.432 \AA$ and a $\mathrm{C}-\mathrm{C}-\mathrm{O}$ angle of $127.9^{\circ}$. The $\mathrm{C}-\mathrm{O}$ bond length of $\mathbf{T} \mathbf{2}$ is about $0.03 \AA$ longer than that in $\mathbf{S 2}$. However, the $\mathrm{C}-\mathrm{H}$ distances are very similar in $\mathbf{S 2}$ and $\mathbf{T 2}$. Triplet $\mathbf{T 2 2}\left({ }^{3} \mathrm{~A}_{2}\right)$ has the same atomic arrangement as $\mathbf{S 2}$; its $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}-\mathrm{C}$ bond lengths are longer than those of S2 ( 0.049 and $0.081 \AA$ longer, respectively). The C atom end-on attack structures, $\mathbf{S 6 6}\left({ }^{1} \mathrm{~A}_{1}\right), \mathbf{S r} 7\left({ }^{1} \mathrm{~A}_{2}\right)$, and $\mathbf{T 5 5}$ $\left({ }^{3} \mathrm{~A}_{2}\right)$, are found to be transition states with one imaginary frequency and display distinct structural characteristics. Singlet S66 has the shortest C-O bond length ( $1.180 \AA$ ) and the longest $\mathrm{C}-\mathrm{C}$ bond $(1.362 \AA$ ), while the structures of $\mathbf{S r} 7$ and $\mathbf{T 5 5}$ are rather similar to each other. The stationary structures $\mathbf{S r} 7$ and S7p have two imaginary frequencies, and $\mathbf{S 7}$ has one imaginary frequency. Distortions along the smaller imaginary frequency, which is out-of-plane bending, lead to real transition states or minimum with lower symmetry at the DFT level. However, the stationary points are close to the higher-symmetry species and, after zero-point correction, the higher-symmetry species are lower in energy. Thus, we considered $\mathbf{S r} 7$ and $\mathbf{S 7 p}$ as transition states and $\mathbf{S 7}$ as a minimum despite the wrong number of imaginary frequencies and used the higher-symmetry structures
for geometry optimization at the CAS level. The singlet and triplet carbene ( $\mathbf{S 3}$ and $\mathbf{T 4}$ ) intermediates are also characterized. Structurally, both are similar except that $\mathbf{S 3}$ has an OCCH dihedral angle of $82.6^{\circ}$ while T4 is planar. On the singlet surface, several carbenes similar to $\mathbf{S 3}$ are identified at the DFT level; among them, we chose the one with the lowest free energy for CAS-level thermodynamic corrections. The geometries of four lowest-energy states of methylene $\left({ }^{3} \mathrm{~B}_{1},{ }^{1} \mathrm{~A}_{1},{ }^{1} \mathrm{~B}_{1}\right.$, and $\mathrm{c}^{1} \mathrm{~A}_{1}$, Figure 3) are close to those reported in the literature. ${ }^{30,31}$

Calculated relative energies ( $\mathrm{kcal} / \mathrm{mol}$ ) are given in Tables 2 and 3 for triplet and singlet species, respectively, and the schematic free energy surfaces for each multiplicity are given in Figures 4 and 5. In the discussion, we will use $\Delta G_{298}$, which is the MCPT electronic energy, with ZPC, heat capacity $\left(C_{\mathrm{p}}\right)$, and entropy $(\Delta S)$ corrections at the DFT level. On the triplet free energy surface (Figure 4), $\mathbf{T} \mathbf{2}$ is the lowest-energy species, $-91.1 \mathrm{kcal} / \mathrm{mol}$ relative to $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{3} \mathrm{P}\right)$. The addition of a

[^3]

Figure 2. Optimized geometries of triplet species at the DFT (PBE1PBE/6-311++G(3df,p)) and CAS (CAS(14,13)/6-311+G(2d,p)) (in italic) levels. Literature values (underlined) for $\mathbf{T} \mathbf{2}$ are from ref 18 b . Bond lengths are in angstroms and angles are in degrees.

C atom to the $\mathrm{C}-\mathrm{O} \pi$ bond initially forms a triplet oxiranylidene T1 without barrier. $\mathbf{T 1}$ can undergo $\mathrm{H}_{2} \mathrm{C}-\mathrm{O}$ bond-breaking, $\mathrm{C}-\mathrm{C}$ bond-breaking, or hydrogen transfer to oxygen or to carbon. All four pathways were examined, but no transition state for hydrogen transfer to oxygen was found. The lowest-energy pathway leads to $\mathbf{T} \mathbf{2}$ on the triplet surface, with a free energy barrier of $14.5 \mathrm{kcal} / \mathrm{mol}$ and a reaction free energy of -66.3 $\mathrm{kcal} / \mathrm{mol}$. There must be a valley-ridge inflection (VRI) points or a bifurcation along the $\mathrm{H}_{2} \mathrm{C}-\mathrm{O}$ bond-breaking ( $\mathbf{T} \mathbf{\rightarrow} \boldsymbol{T} 2$ ), ${ }^{33}$ because a $\mathrm{C}-\mathrm{O}$ stretching mode cannot directly connect two minima ( $\mathbf{T 1}$ and $\mathbf{T 2}$ ); a rotation or bending mode is also necessary. At a VRI point along the $\mathrm{C}-\mathrm{C}-\mathrm{O}$ opening coordinate, the eigenvalue of the $\mathrm{C}-\mathrm{O}$ stretching vector becomes zero and the rotational mode around the $\mathrm{C}-\mathrm{C}$ bond becomes imaginary. Therefore, there are two saddle points along the $C_{s}$

[^4]symmetry coordinate, $\mathbf{T 1 2}$ with a $\mathrm{C}-\mathrm{O}$ stretching transition vector and $\mathbf{T} 22$ with a rotation transiton vector around the $\mathrm{C}-\mathrm{C}$ bond.

Other dissociation pathways are not studied in detail. The free energies ( 298 K ) of products show that, on the triplet free energy surface, the formation of CO plus methylene is the dominant pathway and the dissociation to oxygen $\left.\left(\mathrm{O}^{( }{ }^{3} \mathrm{P}\right)\right)$ and acetylene $(-29.0 \mathrm{kcal} / \mathrm{mol})$ is much higher in free energy than methylene formation ( $-78.2 \mathrm{kcal} / \mathrm{mol}$ ). The hydrogen extrusion might be a competitive channel ( $-50.0 \mathrm{kcal} / \mathrm{mol}$ ), and this would lead to other products. This part of the PES has already been studied in detail, ${ }^{23 f, g}$ and we are in good agreement with previous results.

Ketene T2 can undergo two interconversions: a rotation around the $\mathrm{C}-\mathrm{C}$ bond ( $8.5 \mathrm{kcal} / \mathrm{mol}$ free energy barrier) and an inversion via a linear $\mathrm{C}-\mathrm{C}-\mathrm{O}$ structure ( $\mathbf{T 2 2}^{\prime}, 27.0 \mathrm{kcal} /$ mol barrier). It is also possible to transfer a hydrogen atom to the other carbon to form a triplet carbene (T4), though the free energy barrier is quite unfavorable ( $58.0 \mathrm{kcal} / \mathrm{mol}$ ). The fate of T4 is not clear. Breaking the $\mathrm{C}-\mathrm{C}$ bond to yield CH and HCO is very unfavorable ( $75.1 \mathrm{kcal} / \mathrm{mol}$ free energy barrier). There-

Table 1. Calculated Electronic Energies (au) at the DFT, CAS, and MCPT Levels along with ZPC (kcal/mol), $H_{\text {corr }}$ (kcal/mol), Entropy (S, $\mathrm{cal} / \mathrm{K} \cdot \mathrm{mol})$, DFT Spin-Squared Value $\left(\left\langle S^{2}\right\rangle\right)$, CAS Reference Weight of Dominant Configuration ( $c_{i}^{2}$ ), and Electronic States

|  | ZPC | $\mathrm{H}_{\text {corr }}$ | $S$ | $\left\langle S^{2}\right\rangle$ | $c_{i}^{2}$ | state | DFT | CAS | MCPT |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ | 0.0 | 1.5 | 35.6 | 2.00 |  | ${ }^{3} \mathrm{P}$ | -37.80321 | -37.70299 | -37.76948 |
| C ( ${ }^{1} \mathrm{D}$ ) | 0.0 | 1.5 | 33.4 | 1.01 |  | ${ }^{1} \mathrm{D}$ | -37.78825 | -37.64525 | -37.71821 |
| $\mathrm{C}\left({ }^{1} \mathrm{~S}\right)$ | 0.0 | 1.5 | 33.4 | 0.00 |  | ${ }^{1} \mathrm{~S}$ | -37.73128 | -37.60755 | -37.67319 |
| CO | 3.2 | 5.3 | 47.2 | 0.00 |  | ${ }^{1} \Sigma$ | -113.22500 | -112.90363 | -113.09712 |
| $\mathrm{CH}_{2} \mathrm{O}$ | 16.8 | 19.2 | 52.2 | 0.00 |  | ${ }^{1} \mathrm{~A}_{1}$ | -114.41299 | -114.03723 | -114.25908 |
| $\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ | 10.9 | 13.3 | 46.6 | 2.01 | 0.97 | ${ }^{3} \mathrm{~B}_{1}$ | -39.11334 | -38.96922 | -39.04985 |
| $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ | 10.5 | 12.8 | 45.2 | 0.00 | 0.92 | ${ }^{1} \mathrm{~A}_{1}$ | -39.08598 | -38.95214 | -39.02520 |
| $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ | 10.8 | 13.2 | 45.0 | 0.79 | 0.48 | ${ }^{1} \mathrm{~B}_{1}$ | -39.09191 | -38.90222 | -38.99299 |
| $\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)^{a}$ | 10.6 | 13.0 | 42.0 |  | 0.49 | ${ }^{1} \mathrm{~A}_{1}$ |  | -38.85490 | -38.95163 |
| CH | 4.1 | 6.2 | 42.3 | 0.75 | 0.49 | ${ }^{2} \Pi$ | -38.43636 | -38.31836 | -38.38820 |
| HCO | 8.3 | 10.6 | 53.6 | 0.75 | 0.94 | ${ }^{2} \mathrm{~A}^{\prime}$ | -113.76579 | -113.40462 | -113.62390 |
| S1 | 20.4 | 22.9 | 58.3 | 0.00 | 0.90 | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.37894 | -151.86774 | -152.15813 |
| S2 | 19.9 | 22.7 | 57.7 | 0.00 | 0.90 | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.48037 | -151.96541 | -152.26748 |
| S2" | 19.6 | 22.3 | 59.5 | 1.02 | 0.40 | ${ }^{1} \mathrm{~A}^{\prime \prime}$ | -152.39395 | -151.86882 | -152.17944 |
| S3 | 17.6 | 20.9 | 63.4 | 0.66 | 0.86 | ${ }^{1} \mathrm{~A}$ | -152.35063 | -151.83978 | -152.13372 |
| S4 | 18.7 | 21.6 | 59.5 | 0.00 | 0.88 | ${ }^{1} \mathrm{~A}_{1}$ | -152.35261 | -151.82673 | -152.14154 |
| S5 | 20.1 | 23.1 | 59.0 | 0.00 | 0.90 | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.42108 | -151.90656 | -152.21047 |
| $\mathbf{S 6}^{\text {b }}$ | 18.6 | 21.6 | 60.9 | 0.00 |  | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.31492 |  |  |
| S7 ${ }^{\text {c }}$ | 17.5 | 20.4 | 60.1 | 1.01 | 0.46 | ${ }^{1} \mathrm{~A}^{\prime \prime}$ | -152.29307 | -151.78186 | -152.06890 |
| S12 | 17.5 | 20.3 | 60.7 | 0.55 | 0.12 | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.34339 | -151.83313 | -152.13225 |
| S13 | 16.8 | 19.3 | 58.6 | 0.00 | 0.88 | ${ }^{1} \mathrm{~A}$ | -152.29228 | -151.76894 | -152.07458 |
| S15 | 15.8 | 18.4 | 58.8 | 0.00 | 0.89 | ${ }^{1} \mathrm{~A}$ | -152.26001 | -151.74954 | -152.03200 |
| S2"2" | 18.0 | 20.6 | 57.1 | 1.02 | 0.31 | ${ }^{1} \mathrm{~A}_{2}$ | -152.36022 | -151.83125 | -152.14786 |
| S23 | 17.2 | 20.0 | 59.8 | 0.64 | 0.89 | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.35024 | -151.83890 | -152.13009 |
| S25 | 16.0 | 19.1 | 60.6 | 0.00 | 0.83 | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.32577 | -151.79756 | -152.12003 |
| S34 | 18.4 | 21.0 | 59.2 | 0.00 | 0.84 | ${ }^{1} \mathrm{~A}$ | -152.35046 | -151.84396 | -152.13308 |
| S66 | 18.4 | 21.2 | 57.9 | 0.00 | 0.87 | ${ }^{1} \mathrm{~A}_{1}$ | -152.31127 | -151.79402 | -152.09282 |
| S6p ${ }^{\text {b }}$ | 17.5 | 20.6 | 61.4 | 0.00 |  | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.31396 |  |  |
| S7p ${ }^{\text {c }}$ | 15.9 | 19.2 | 64.0 | 1.00 | 0.41 | ${ }^{1} \mathrm{~A}^{\prime}$ | -152.27168 | -151.73690 | -152.05775 |
| Sr7 ${ }^{\text {c }}$ | 17.2 | 20.2 | 59.7 | 1.01 | 0.37 | ${ }^{1} \mathrm{~A}_{2}$ | -152.26256 | -151.73876 | -152.03349 |
| $\mathbf{S}_{\mathbf{c i}}{ }^{d}$ | 19.6 | 22.3 | 59.5 |  |  |  |  | -151.84950 | -152.16824 |
| T1 | 20.1 | 22.7 | 60.6 | 2.01 | 0.91 | ${ }^{3} \mathrm{~A}$ " | -152.29621 | -151.76542 | -152.08428 |
| T2 | 19.1 | 21.9 | 62.2 | 2.01 | 0.16 | ${ }^{3} \mathrm{~A}$ " | -152.39793 | -151.87873 | -152.18798 |
| T3 | 19.6 | 22.2 | 59.2 | 2.01 | 0.91 | ${ }^{3} \mathrm{~B}$ | -152.32432 | -151.78806 | -152.10321 |
| T4 | 19.0 | 21.7 | 61.9 | 2.03 | 0.90 | ${ }^{3} \mathrm{~A}$ " | -152.36686 | -151.85794 | -152.15574 |
| T5 | 17.9 | 21.0 | 63.5 | 2.01 | 0.06 | ${ }^{3} \mathrm{~A}$ " | -152.29754 | -151.79195 | -152.07875 |
| T6 | 17.1 | 20.1 | 63.5 | 2.01 | 0.90 | ${ }^{3} \mathrm{~A}$ " | -152.24274 | -151.74531 | -152.02303 |
| T7 | 19.0 | 21.8 | 62.0 | 2.01 | 0.84 | ${ }^{3} \mathrm{~A}$ " | -152.31178 | -151.77501 | -152.10270 |
| T12 | 19.6 | 22.0 | 60.5 | 2.13 | 0.03 | ${ }^{3} \mathrm{~A}$ " | -152.26744 | -151.73773 | -152.06021 |
| T13 | 16.3 | 18.9 | 60.8 | 2.01 | 0.89 | ${ }^{3} \mathrm{~A}$ | -152.24172 | -151.70055 | -152.02343 |
| T15 | 17.1 | 20.1 | 65.2 | 2.01 | 0.80 | ${ }^{3} \mathrm{~A}$ " | -152.25769 | -151.75622 | -152.04323 |
| T22 | 18.0 | 20.7 | 61.7 | 2.01 | 0.91 | ${ }^{3} \mathrm{~A}^{\prime}$ | -152.38049 | -151.86024 | -152.17257 |
| T24 | 15.4 | 18.2 | 61.7 | 2.02 | 0.87 | ${ }^{3} \mathrm{~A}$ | -152.30075 | -151.77008 | -152.08981 |
| T27 | 15.0 | 17.7 | 61.4 | 2.02 | 0.51 | ${ }^{3} \mathrm{~A}$ " | -152.23731 | -151.71033 | -152.02596 |
| T2p | 15.0 | 18.9 | 72.0 | 2.01 | 0.84 | ${ }^{3} \mathrm{~A}$ " | -152.33779 | -151.84749 | -152.14815 |
| T34 | 17.6 | 20.2 | 61.2 | 2.01 | 0.74 | ${ }^{3} \mathrm{~A}$ | -152.28006 | -151.75141 | -152.07125 |
| T56 | 15.0 | 17.7 | 61.5 | 2.02 | 0.84 | ${ }^{3} \mathrm{~A}$ " | -152.22171 | -151.69994 | -152.02092 |
| T5p | 15.5 | 18.9 | 66.4 | 2.02 | 0.64 | ${ }^{3} \mathrm{~A}$ " | -152.28497 | -151.77296 | -152.08015 |
| T22' | 18.0 | 20.7 | 59.2 | 2.01 | 0.91 | ${ }^{3} \mathrm{~A}_{2}$ | -152.36096 | -151.82249 | -152.14431 |
| T55 | 17.3 | 20.2 | 61.3 | 2.02 | 0.64 | ${ }^{3} \mathrm{~A}_{2}$ | -152.26537 | -151.71934 | -152.03924 |

${ }^{a}$ Thermodynamic correction data are obtained at the CAS level, because we could not locate the excited $\mathrm{c}^{1} \mathrm{~A}_{1}$ minimum at the DFT level. ${ }^{b}$ At the CAS level, a stationary point for $\mathbf{S 6 p}$ could not be found. At the DFT level, after the zero-point energy correction, the relative energy order of the minimum (S6) and the transition state ( $\mathbf{S} \mathbf{6 p}$ ) becomes reversed. We conclude, therefore, that $\mathbf{S 6}$ will not exist on the potential energy surface. ${ }^{c}$ The three indicated structures have an "extra" imaginary frequency that corresponds to out-of-plane distortion. When the true transition states ( $\mathbf{S r} 7$ and $\mathbf{S 7 p}$ ) and minimum ( $\mathbf{S 7}$ ) were located in $C_{1}$ symmetry at the DFT level, zero-point corrections reversed the relative energies with the corresponding higher-symmetry $\left(C_{s}\right)$ structures. For that reason, $C_{s}$ symmetry was used for the CAS level geometry optimization. ${ }^{d}$ Single-point energy calculations at the CAS and MCPT levels are performed for both the ${ }^{1} \mathrm{~A}^{\prime}$ and ${ }^{1} \mathrm{~A}^{\prime \prime}$ states on the geometry obtained from conical intersection optimization at the $\mathrm{CAS}(6,6) / 6-311+\mathrm{G}(2 \mathrm{~d}, \mathrm{p})$ level. The energy reported is the average of both states. Thermodynamic corrections of $\mathbf{S} \mathbf{2}^{\prime \prime}$ are used for the enthalpy and free energy corrections of the conical intersection structure.
fore, $\mathbf{T 4}$ most likely will undergo reactions with reactants (i.e., $\mathrm{CH}_{2} \mathrm{O}$ ). The pathway we are most interested in for $\mathbf{T} 2$ is breaking the $\mathrm{C}-\mathrm{C}$ bond to form carbon monoxide and tripletstate methylene ( ${ }^{3} \mathrm{~B}_{1}$ ) with a $19.0 \mathrm{kcal} / \mathrm{mol}$ free energy barrier (reverse barrier, $6.1 \mathrm{kcal} / \mathrm{mol}$ ). This result is in good agreement with those reported by Allen et al. ${ }^{18 \mathrm{~b}}$ The $\mathrm{C}-\mathrm{C}$ bond dissociation energy $\left(\Delta H_{0}=20.7 \mathrm{kcal} / \mathrm{mol}\right.$, Table 2$)$ is also close to their calculated value $(18.6 \mathrm{kcal} / \mathrm{mol})$ and the proposed value of 22.3 $\mathrm{kcal} / \mathrm{mol} .{ }^{18 \mathrm{~b}}$ The 0 K enthalpy barrier (forward, $20.9 \mathrm{kcal} / \mathrm{mol}$; reverse, $0.2 \mathrm{kcal} / \mathrm{mol}$ ) is somewhat lower than their estimation
(forward, $25-27 \mathrm{kcal} / \mathrm{mol}$; reverse, 3-4 kcal/mol). Thus, the reaction of triplet methylene with $\mathbf{C O}$ to form $\mathbf{T} 2$ has a very low barrier.

In T1, hydrogen transfer to another carbon is not likely to occur due to a $34.3 \mathrm{kcal} / \mathrm{mol}$ free energy barrier. If C atoms have a large amount of kinetic energy, then this barrier could be overcome, which would lead to triplet oxirene, T3, which can transform into a carbene $\mathbf{T 4}$. If $\mathrm{C}-\mathrm{C}$ bond cleavage occurs in $\mathbf{T 1}$, the bent $\mathrm{H}_{2} \mathrm{C}-\mathrm{O}-\mathrm{C}$ (T5) isomer will form. However, T5 will dissociate into CO and $\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ without a free energy


Figure 3. Optimized geometries of the four lowest energy states of methylenes at the DFT and CAS (in italic) levels. Literature values (underlined) are from ref 31. Bond lengths are in angstroms and angles are in degrees.

Table 2. Relative Enthalpies ( $\mathrm{kcal} / \mathrm{mol}$ ) of $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{O}$ Triplet Isomers at $0 \mathrm{~K}\left(\Delta H_{0}\right)$ and $298 \mathrm{~K}\left(\Delta H_{298}\right)$ and Free Energies at 298 K $\left(\Delta G_{298}\right)$ Calculated at the MCPT Level with Thermodynamic Corrections at the DFT Level ${ }^{a}$

|  | $\Delta H_{0}$ | $\Delta H_{298}$ |  | $\Delta G_{298}$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  | calc | $\exp$ |  |
| $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ | 0.0 | 0.0 | 0.0 | 0.0 |
| $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ | 32.2 | 32.2 | $29.1{ }^{\text {b }}$ | 32.8 |
| $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{1} \mathrm{~S}\right)$ | 60.4 | 60.4 | $61.9{ }^{\text {b }}$ | 61.1 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ | -77.0 | -76.4 | $-76.7^{c}$ | -78.2 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ | -61.9 | -61.3 | $-67.7^{c}$ | -62.7 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ | -41.4 | -41.4 | $-43.8{ }^{\text {c }}$ | -42.3 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$ | -18.8 | -17.4 | $-16.6^{c}$ | -15.8 |
| $\mathrm{CH}+\mathrm{HCO}$ | 5.9 | 6.5 | $8.2{ }^{\text {d }}$ | 4.1 |
| T1 | -31.6 | -32.9 |  | -24.8 |
| T2 | -97.7 | -98.7 |  | -91.1 |
| T3 | -44.0 | -45.3 |  | -36.8 |
| T4 | -77.5 | -78.7 |  | -71.0 |
| T5 | -30.4 | -31.2 |  | -23.9 |
| T6 | 5.3 | 4.5 |  | 11.8 |
| T7 | -44.3 | -45.4 |  | -37.7 |
| T12 | -17.0 | -18.5 |  | -10.2 |
| T13 | 2.8 | 1.4 |  | 9.5 |
| T15 | -8.9 | -9.7 |  | -3.0 |
| T22 | -89.1 | -90.3 |  | -82.6 |
| T24 | -39.8 | -40.9 |  | -33.1 |
| T27 | -0.1 | -1.3 |  | 6.5 |
| T2p | -76.8 | -76.8 |  | -72.1 |
| T34 | -25.9 | -27.2 |  | -19.3 |
| T56 | 3.1 | 1.9 |  | 9.7 |
| T5p | -33.6 | -34.1 |  | -27.7 |
| Tv1 | -71.4 | -72.6 |  | -64.1 |
| n | -5.5 | -6.5 |  | 0.8 |

${ }^{a}$ All thermodynamic values are relative to $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{3} \mathrm{P}\right) .{ }^{b}$ The experimental $\Delta H_{298}$ values for $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ and $\mathrm{CH}_{2} \mathrm{O}$ are taken as 171.3 and $-27.7 \mathrm{kcal} / \mathrm{mol}$, respectively. Relative energies are calculated by using the data from ref $2 .^{c}$ A value of $93.3 \mathrm{kcal} / \mathrm{mol}$ was used for $\Delta H_{298}$ of triplet methylene from ref 32 . The energy separations ${ }^{3} \mathrm{~B}_{1}-{ }^{1} \mathrm{~A}_{1}(9.0 \mathrm{kcal} / \mathrm{mol}$, ref 31b), ${ }^{3} \mathrm{~B}_{1}-{ }^{1} \mathrm{~B}_{1}\left(32.9 \mathrm{kcal} / \mathrm{mol}\right.$, ref 31c), and ${ }^{3} \mathrm{~B}_{1}-\mathrm{c}^{1} \mathrm{~A}_{1}(60.1 \mathrm{kcal} / \mathrm{mol}$, ref 31a) were used to determine the $\Delta H_{298}$ of the excited states of methylene. ${ }^{d}$ An experimental value of $10.0 \mathrm{kcal} / \mathrm{mol}$ for the $\Delta H_{298}$ of CHO was used from ref 32.
barrier. T5p was located as a transition state at both the DFT and CAS levels, but at the MCPT level the energy is lower than that of T5. A transition state $\mathbf{T 5 5}$ was located as the inversion transition for $\mathbf{T 5}$.

It is known experimentally that triplet C atoms abstract hydrogen atoms from organic compounds. ${ }^{1}$ On this surface, no transition state could be located for hydrogen abstraction, which is nonspontaneous ( $\left.\Delta G_{298}=4.1 \mathrm{kcal} / \mathrm{mol}\right)$ and proceeds without

Table 3. Relative Enthalpies ( $\mathrm{kcal} / \mathrm{mol}$ ) of $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{O}$ Singlet Isomers at $0 \mathrm{~K}\left(\Delta H_{0}\right)$ and $298 \mathrm{~K}\left(\Delta H_{298}\right)$ and Free Energies at 298 K $\left(\Delta G_{298}\right)$ Calculated at the MCPT Level with Thermodynamic Corrections at the DFT Level ${ }^{a}$

|  | $\Delta H_{0}$ | $\Delta H_{298}$ |  | $\Delta G_{298}$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  | calc | exp |  |
| $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ | 0.0 | 0.0 | 0.0 | 0.0 |
| $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ | 32.2 | 32.2 | 29.1 | 32.8 |
| $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{1} \mathrm{~S}\right)$ | 60.4 | 60.4 | 61.9 | 61.1 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ | -77.0 | -76.4 | -76.7 | -78.2 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ | -61.9 | -61.3 | -67.7 | -62.7 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ | -41.4 | -41.4 | -43.8 | -42.3 |
| $\mathrm{CO}+\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$ | -18.8 | -17.4 | -16.6 | -15.8 |
| $\mathrm{CH}\left({ }^{2} \Pi\right)+\mathrm{HCO}\left({ }^{2} \mathrm{~A}^{\prime}\right)$ | 5.9 | 6.5 | 8.2 | 4.1 |
| S1 | -77.7 | -79.0 |  | -70.2 |
| S2 | -146.8 | -147.9 | $-155.0^{b}$ | -138.9 |
| S2" | -91.9 | -93.0 |  | -84.6 |
| S3 | -65.1 | -65.7 |  | -58.5 |
| S4 | -69.0 | -69.9 |  | -61.5 |
| S5 | -110.8 | -111.7 |  | -103.1 |
| S7 | -25.7 | -26.8 |  | -18.5 |
| S12 | -64.4 | -65.4 |  | -57.3 |
| S13 | -28.9 | -30.2 |  | -21.5 |
| S15 | -3.1 | -4.4 |  | 4.2 |
| S23 | -63.2 | -64.4 |  | -56.0 |
| S25 | -58.2 | -58.9 |  | -50.8 |
| S34 | -64.0 | -65.2 |  | -56.7 |
| S66 | -38.7 | -39.8 |  | -30.8 |
| S7p | -19.1 | -19.7 |  | -12.6 |
| Sr7 | -2.7 | -3.5 |  | 4.9 |
| $\mathrm{S}_{\text {ci }}$ | -84.8 | -86.0 |  | -77.5 |

${ }^{a}$ All thermodynamic values are relative to $\mathrm{CH}_{2} \mathrm{O}+\mathrm{C}\left({ }^{3} \mathrm{P}\right)$. For the detailed explanation, see Table $2 .{ }^{b}$ A value of $11.4 \mathrm{kcal} / \mathrm{mol}$ from ref 32 was used for $\Delta H_{298}$ of the ground state of ketene ( $\mathbf{S 2}$ ) to calculate relative enthalpies.
a reverse barrier. There is ample evidence that $\mathrm{C}-\mathrm{H}$ abstractions by radicals have low activation barriers. For example, hydrogen abstractions from formaldehyde by halogen atoms are almost barrierless (for Cl ) at the $\operatorname{CCSD}(\mathrm{T}) / / \mathrm{B} 3 \mathrm{LYP} / 6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$ level ${ }^{34 \mathrm{a}}$ and have very low barriers ( 8.5 and $4.4 \mathrm{kcal} / \mathrm{mol}$ for F and Cl , respectively) at the MP2/aug-cc-pVDZ level. ${ }^{34 \mathrm{~b}}$ In this context, it is not surprising that the hydrogen abstraction from formaldehyde by $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ proceeds without reverse barrier. In addition, as shown in eq 2, no electron rearrangement is necessary to produce two ground-state products in this reaction.


On the singlet PES (Figure 5), the most probable reaction between $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ with formaldehyde is also $\pi$ addition to form $\mathbf{S 1}$. This reaction is $103.0 \mathrm{kcal} / \mathrm{mol}$ exoergic, and $\mathbf{S} 1$ will have enough energy to undergo further reaction. The lowest energy reaction path is to form ground state $\mathbf{S} 2\left({ }^{1} \mathrm{~A}_{1}\right)$ via $\mathbf{S 1 2}$ over a $12.9 \mathrm{kcal} / \mathrm{mol}$ free energy barrier by breaking the $\mathrm{H}_{2} \mathrm{C}-\mathrm{O}$ bond. Another possible path is hydrogen transfer to either carbon or oxygen. Although hydrogen transfer to carbon has a high barrier ( $48.7 \mathrm{kcal} / \mathrm{mol}$ ), the system has enough energy to yield singlet carbene $\mathbf{S 3}$. The singlet carbene, $\mathbf{S 3}$, can easily convert into $\mathbf{S 2}$ ( $2.5 \mathrm{kcal} / \mathrm{mol}$ barrier). It can also make a $\mathrm{C}-\mathrm{O}$ bond to form oxirene, $\mathbf{S 4}$. Our results are in good agreement with a number

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Figure 4. Triplet free energy surface constructed from $\Delta G_{298}$ at the MCPT level. The free energies of singlet $\mathrm{H}_{2} \mathrm{CCO}\left({ }^{1} \mathrm{~A}^{\prime \prime}\right.$ and $\left.{ }^{1} \mathrm{~A}^{\prime}\right)$ are computed at the $\mathbf{T} 2\left({ }^{3} \mathrm{~A}^{\prime \prime}\right)$ geometry. Relative energies are given in kilocalories per mole.


Figure 5. Singlet free energy surface constructed from $\Delta G_{298}$ at the MCPT level. $\mathbf{S}_{\mathrm{ci}}$ is the crossing geometry between the ${ }^{1} \mathrm{~A}^{\prime}$ and ${ }^{1} \mathrm{~A}^{\prime \prime}$ surfaces (see text). Relative energies are given in kilocalories per mole.
of studies which have been performed on the singlet oxirene rearrangement mechanism (Wolff rearrangement). ${ }^{23}$ Singlet S3 is lower than $\mathbf{S 4}$ in free energy at the CAS level, but the energy order is reversed at the MCPT level. A similar disagreement has been reported between the MP2 and CCSD(T) levels, where the singlet carbene ( $\mathbf{S 3}$ ) is a minimum at the $\operatorname{CCSD}(\mathrm{T})$ level but not at the MP2 level. ${ }^{23 b, e}$ The authors ${ }^{23 e}$ felt that truncation
after the second-order term in perturbation theory was responsible for the poor description of the singlet carbene, $\mathbf{S 3}$.

In S1, hydrogen transfer to oxygen to form $\mathbf{S 5}$ has a high free energy barrier ( $74.4 \mathrm{kcal} / \mathrm{mol}$ ). Singlet $\mathbf{S 5}$ has a collinear $\mathrm{H}-\mathrm{C}-\mathrm{C}-\mathrm{O}$ arrangement, and it is the second lowest species on the free energy surface. A transition state between S2 and $\mathbf{S 5}$ has also been located. Surprisingly, a hydrogen atom moves
directly from oxygen to the end carbon without forming an intervening intermediate. The thermodynamic advantage of making a $\mathrm{C}=\mathrm{O}$ double bond might be the driving force of this process at the expense of a $\mathrm{C} \equiv \mathrm{C}$ triple bond.

In S1, the $\mathrm{C}-\mathrm{C}$ bond-breaking process is complicated. Opening the $\mathrm{C}-\mathrm{C}$ bond will lead to $\mathbf{S 6 6}\left({ }^{1} \mathrm{~A}_{1}\right)$, which has an out-of-plane bending mode of two hydrogen atoms as a transition vector. At the DFT level, a minimum and a transition state were located, but after zero-point energy corrections, the transition state has a lower energy than the minimum. At the CAS level, no minimum was located, and distortion along the transition vector led directly to dissociation of ketene to $\mathrm{CO}+$ $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$. Another way to form $\mathbf{S 6 6}$ is direct addition of the C atom to oxygen. This pathway has no barrier and will lead to either the ${ }^{1} \mathrm{~A}_{1}$ methylene $(+\mathrm{CO})$ or $\mathbf{S} \mathbf{1}$.

On the singlet PES, two pathways which lead to formation of the ${ }^{1} B_{1}$ methylene were found. One starts from direct attack of $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ on oxygen to form $\mathbf{S r} 7\left({ }^{1} \mathrm{~A}_{2}\right)$, which is a transition state for interconversion of $\mathbf{S 7}\left({ }^{1} \mathrm{~A}^{\prime \prime}\right)$. Singlet $\mathbf{S 7}$ dissociates via a $5.9 \mathrm{kcal} / \mathrm{mol}$ free energy barrier to give CO and singlet excited methylene ( ${ }^{1} \mathbf{B}_{1}$ ). These three ( $\mathbf{S r} 7, \mathbf{S} 7$, and $\mathbf{S 7 p}$ ) are biradical species on the ${ }^{1} \mathrm{~A}^{\prime \prime}$ surface.

The central question is whether ${ }^{1} \mathrm{~B}_{1}$ methylene can be formed on the ${ }^{1} \mathrm{~A}^{\prime \prime}$ surface. The ${ }^{1} \mathrm{D}$ state has five microstates which will split into two $\mathrm{A}_{1}$ and one $\mathrm{A}_{2}, \mathrm{~B}_{1}$, and $\mathrm{B}_{2}$ states in $C_{2 v}$ symmetry, and into three $\mathrm{A}^{\prime}$ and two $\mathrm{A}^{\prime \prime}$ states in $C_{s}$ symmetry. When the ${ }^{1} \mathrm{D}$ carbon attacks the formaldehyde oxygen atom, the microstates will split into three ${ }^{1} \mathrm{~A}^{\prime}$ and two ${ }^{1} \mathrm{~A}^{\prime \prime}$ states, and the ratio between states of $\mathrm{A}^{\prime}$ and $\mathrm{A}^{\prime \prime}$ symmetry will be 3:2. Thus, reactions on the $A^{\prime \prime}$ surface are certainly possible. The next question to consider is whether this deoxygenation process is faster than intersystem crossing (ISC). The quantitative answer to this question cannot be obtained from this study, but it can be answered qualitatively. The dissociation will proceed very quickly, since it has only a $5.9 \mathrm{kcal} / \mathrm{mol}$ barrier, and the system will have about $50 \mathrm{kcal} / \mathrm{mol}$ extra energy at $\mathbf{S 7}$. The ISC occurs along the seam of two potential energy surfaces if the spinorbit coupling is large enough and the geometries are similar to each other. ${ }^{35-39}$ Generally speaking, the spin-orbit coupling is large in heavier elements, but in the first-row elements the spin-orbit coupling is very small. ${ }^{36,38}$ One example of a tripletsinglet intersystem crossing rate has been reported in $\mathrm{CF}_{2} \mathrm{CF}_{2}-\mathrm{O}$ as $4 \times 10^{12} \mathrm{~s}^{-1} \cdot{ }^{40}$ The rate of ISC in $\mathrm{COCH}_{2}$ may be similar to that in $\mathrm{CF}_{2} \mathrm{CF}_{2}-\mathrm{O}$ since the energy gap between the ${ }^{1} \mathrm{~A}^{\prime \prime}$ and ${ }^{3} \mathrm{~A}^{\prime \prime}$ surfaces is also small ( $\mathbf{S 7} \mathbf{- T 5}: \Delta G=5.4 \mathrm{kcal} / \mathrm{mol}$, from Tables 2 and 3). Thus, the excited singlet species ( ${ }^{1} \mathrm{~A}^{\prime \prime}$ ) should undergo rapid ISC to the lower ${ }^{3} \mathrm{~A}^{\prime \prime}$ surface. However, $\mathrm{F}_{2} \mathrm{CF}_{2}-$ CO differs from $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ in that it is a biradical with a radical center on oxygen, and this factor may be responsible for the rapid ISC observed in this species. In the present reaction, we suggest that the formation of ${ }^{1} \mathrm{~B}_{1}$ methylene via the ${ }^{1} \mathrm{~A}^{\prime \prime}$ surface $(\mathbf{S r} 7 \rightarrow \mathbf{S 7} \rightarrow \mathbf{S 7 p}$ ) can occur only if ISC is slow relative to dissociation. Therefore, we suggest that the formation of ${ }^{1} \mathrm{~B}_{1}$

[^6]Table 4. Important Valence Electron Configurations of the Four Lowest Electronic State Methylenes and Four Singlet Species Obtained at the CAS Level

|  | configuration | $\left.\|c\|\right\|^{b}$ |
| :---: | :---: | :---: |
| $\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ | $\mathrm{a}_{1}{ }^{2} \mathrm{~b}_{2}{ }^{2} \mathrm{a}_{1} \mathrm{~b}_{1}$ | 0.98 |
| $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ | $\begin{aligned} & a_{1}{ }^{2} b_{2}^{2} a_{1} a_{1}^{2} \\ & a_{1}{ }^{2} b_{2}^{2} b_{1}^{2} b_{1}^{2} \end{aligned}$ | $\begin{aligned} & 0.97 \\ & 0.18 \end{aligned}$ |
| $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ | $\begin{aligned} & \mathrm{a}_{1}{ }^{2} \mathrm{~b}_{2}{ }^{2} \mathrm{a}_{1} \overline{\mathrm{~b}}_{1} \\ & \mathrm{a}_{1}{ }^{2} \mathrm{~b}_{2}^{2}{ }^{2} \mathrm{a}_{1} \mathrm{~b}_{1} \end{aligned}$ | $\begin{aligned} & 0.70 \\ & 0.70 \end{aligned}$ |
| $\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$ | $\begin{aligned} & a_{1}{ }^{2} b_{2}^{2} b_{1}{ }^{2} \\ & a_{1}{ }^{2} b_{2}^{2} a_{1}^{2} a_{1}^{2} \end{aligned}$ | $\begin{aligned} & 0.73 \\ & 0.67 \end{aligned}$ |
| S2 ( ${ }^{1} \mathrm{~A}_{1}$ ) | $a_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} a_{1}{ }^{2} a_{1}{ }^{2} b_{1}{ }^{2} b_{2}{ }^{2} b_{1}{ }^{2}$ $a_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} a_{1}{ }^{2} a_{1}{ }^{2} b_{1}{ }^{2} b_{1}{ }^{2} b_{2}{ }^{2}$ $a_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} a_{1}{ }^{2} a_{1}{ }^{2} b_{1}{ }^{2} b_{2}{ }^{2} b_{1}{ }^{2}$ | $\begin{aligned} & 0.95 \\ & 0.12 \\ & 0.10 \end{aligned}$ |
| S2" $\left.{ }^{1}{ }^{(1)}{ }^{\prime}\right)$ | $\begin{aligned} & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime 2} a^{\prime 2} a^{\prime \prime}-a^{\prime} \\ & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime 2} a^{\prime 2} a^{\prime \prime} a^{\prime} \\ & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime 2} a^{\prime 2} a^{\prime} a^{\prime \prime} \\ & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime 2} a^{\prime 2} a^{\prime \prime} a^{\prime \prime} \end{aligned}$ | $\begin{aligned} & 0.63 \\ & 0.63 \\ & 0.17 \\ & 0.17 \end{aligned}$ |
| $\mathbf{S 6 6}\left({ }^{1} \mathrm{~A}_{1}\right)$ | $\begin{aligned} & a_{1}{ }^{2} a_{1}{ }^{2}{ }^{2} b_{2}{ }^{2} a_{1}{ }^{2} b_{1}{ }^{2} a_{1}{ }^{2}{ }^{2} b_{2}{ }^{2} b_{1}{ }^{2}{ }^{2} a_{1} b_{2}{ }^{2} a_{1}{ }^{2} b_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} b_{2}{ }^{2} \end{aligned}$ | $\begin{aligned} & 0.93 \\ & 0.15 \end{aligned}$ |
| Sr7 $\left({ }^{1} \mathrm{~A}_{2}\right)$ | $a_{1}{ }^{2} a_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} b_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} \underline{b}_{1} \bar{b}_{2}$ $a_{1}{ }^{2} a_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} b_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} b_{1} b_{2}$ $a_{1}{ }^{2} a_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} b_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} b_{1} b_{2}$ $a_{1}{ }^{2} a_{1}{ }^{2} a_{1}{ }^{2} b_{2}^{2} b_{1}{ }^{2} a_{1}{ }^{2} b_{2}{ }^{2} b_{1} b_{2}$ | $\begin{aligned} & 0.61 \\ & 0.61 \\ & 0.29 \\ & 0.29 \end{aligned}$ |
| S7p ( ${ }^{1} \mathrm{~A}^{\prime \prime}$ ) | $\begin{aligned} & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime} a^{\prime \prime} \\ & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime} \\ & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime} \\ & a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime \prime} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime 2} a^{\prime \prime} \end{aligned}$ | $\begin{aligned} & 0.64 \\ & 0.64 \\ & 0.17 \\ & 0.17 \end{aligned}$ |

${ }^{a}$ For clarity, core electron configurations are omitted. Singly occupied $\beta$ orbitals are designated with a bar over the orbital designation. ${ }^{b}$ Absolute value of coefficient of each configuration.
methylene via the ${ }^{1} \mathrm{~A}^{\prime \prime}$ surface $(\mathbf{S r} 7 \rightarrow \mathbf{S 7} \rightarrow \mathbf{S 7 p})$, while possible, should not be a significant process.

The other pathway, which proceeds along a ${ }^{1} \mathrm{~A}^{\prime \prime}$ surface $\left(\mathbf{S 2}^{\prime \prime}\right.$ $\left.\left({ }^{1} \mathrm{~A}^{\prime \prime}\right) \rightarrow \mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)\right)$, starts at $\mathbf{S 1 2}$, a biradical stationary point of ${ }^{1} \mathrm{~A}^{\prime}$ symmetry with strong multireferential character, and breaks symmetry as the reaction proceeds to $\mathbf{S 2}^{\prime \prime}$. While $\mathbf{S 1 2}$ is a transition state at the DFT level, we explored the possibility that $\mathbf{S 1 2}$ might be a second-order stationary point at the CAS level. We optimized the $\mathbf{S 1 2}$ geometry at the CAS$(12,11) / 6-311+G(2 d, p)$ level and computed numerical vibrational frequencies. At this level, S12 was found to be a secondorder saddle point with two distinct imaginary frequencies ( $a^{\prime}$, 320i; a", 164i). Stretching the $\mathrm{H}_{2} \mathrm{C}-\mathrm{O}$ bond in $\mathbf{S} 12$ leads to the global minimum $\mathbf{S} 2$, while rotating around the $\mathrm{C}-\mathrm{C}$ bond leads to $\mathbf{S 2}{ }^{\prime \prime}\left({ }^{1} \mathrm{~A}^{\prime \prime}\right.$ state). The $\mathbf{S 2}{ }^{\prime \prime}$ open-shell carbene is the lowest free-energy species on the ${ }^{1} \mathrm{~A}^{\prime \prime}$ surface and will lead to ${ }^{1} \mathrm{~B}_{1}$ methylene with a 42.3 free energy barrier.

Along the $\mathrm{C}-\mathrm{C}$ bond-breaking pathway ( $\mathbf{S 2}^{\prime \prime} \rightarrow \mathrm{CO}+\mathrm{CH}_{2}-$ $\left({ }^{1} \mathrm{~B}_{1}\right)$ ), a conical intersection $\mathbf{S}_{\mathrm{ci}}$ between the ${ }^{1} \mathrm{~A}^{\prime}$ and ${ }^{1} \mathrm{~A}^{\prime \prime}$ surfaces was found using the $\operatorname{CAS}(6,6) / 6-311+G(2 d, p)$ method. The conical intersection is lower in free energy by $14.8 \mathrm{kcal} /$ mol than the $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ plus CO. This conical intersection allows radiationless decay of $\mathbf{S \mathbf { 2 } ^ { \prime \prime }}$ to $\mathbf{S 2}$. However, if the bond-breaking process of $\mathbf{S 2}^{\prime \prime}$ is fast, it is possible to pass through the conical intersection to form $\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ plus CO , in accordance with Carpenter's nonstatistical dynamic effect. ${ }^{41}$

It is still not clear if the products observed from C $\left({ }^{1} \mathrm{D}\right)$ and formaledhyde could come from other lower-energy intermediates on the singlet PES. Thus, we examined orbital correlations

(a)

(b)

(c)

(d)

(e)


(f)

Figure 6. Orbital crossing diagram for the singlet methylene-producing reactions from $\mathbf{S} 2$ and $\mathbf{S 6 6}$. (a) $\mathbf{S} 2 \rightarrow \mathbf{C O}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$, (b) $\mathbf{S 6 6} \rightarrow \mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$, (c) $\mathbf{S 2} \rightarrow \mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$, (d) $\mathbf{S 6 6} \rightarrow \mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$, (e) $\mathbf{S} \mathbf{2} \rightarrow \mathrm{CO}+\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$, and (f) $\mathbf{S 6 6} \rightarrow \mathrm{CO}+\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$.
between ketene with $C_{2 v}$ symmetry ( $\mathbf{S 2}$ and $\mathbf{S 6 6}$ ) and carbene products (Figure 6). Their valence electron configurations are given in Table 4. Interestingly, neither $\mathbf{S 2}$ nor $\mathbf{S 6 6}$ directly correlates to the lowest ${ }^{1} \mathrm{~A}_{1}$ state methylene plus CO, but both correlate to the third excited $\mathrm{c}^{1} \mathrm{~A}_{1}$ state methylene plus CO. As the $\mathrm{C}-\mathrm{C}(\mathrm{C}-\mathrm{O})$ distance becomes longer in $\mathbf{S 2}$ (S66), the $\mathrm{C}-\mathrm{C}$ antibonding orbital ( $\mathrm{a}_{1}$ ) will be stabilized, but the occupied $\mathrm{b}_{1}$ orbital will be destabilized due to the loss of $\pi$ bonding interaction. As shown in Figure 6, to correlate the ${ }^{1} \mathrm{~A}_{1}$ ketene ( $\mathbf{S 1}$ or $\mathbf{S 6 6}$ ) with the ${ }^{1} \mathrm{~A}_{1}$ methylene plus CO, the orbital crossing between $b_{1}$ and $a_{1}$ orbitals is unavoidable. The correlation diagram between the ${ }^{1} \mathrm{~A}_{1}$ ketene state and the ${ }^{1} \mathrm{~B}_{1}$ methylene state plus CO (Figure $6 \mathrm{c}, \mathrm{d}$ ) also shows a crossing, but the energies of the two orbitals ( $a_{1}$ and $b_{1}$ ) are pseudo-degenerate. The ${ }^{1} \mathrm{~A}_{1}$ state ketene isomers, $\mathbf{S 2}$ and $\mathbf{S 6 6}$, correlate with the excited $\mathrm{c}^{1} \mathrm{~A}_{1}$ methylene plus CO without orbital crossing (Figure $6 \mathrm{e}, \mathrm{f})$. In this case, there must be a transition state in the dissociation pathway of ketene along the $\mathrm{C}-\mathrm{C}$ bond elongation.

The reaction enthalpies and free energies of oxygen abstraction reactions by C atom obtained in this study are summarized in Table 5. Our results are in very good agreement with experimental results. The reaction $\mathrm{C}+\mathrm{CH}_{2} \mathrm{O} \rightarrow \mathrm{CO}+\mathrm{CH}_{2}$ is highly exoergic, and the reaction free energy of the excited

[^7]Table 5. Reaction Enthalpies at $0 \mathrm{~K}\left(\Delta H_{0}\right)$ and $298 \mathrm{~K}\left(\Delta H_{298}\right)$ and Free Energies at $298 \mathrm{~K}\left(\Delta G_{298}\right)$ at the MCPT Level (in kcal/mol)

| reactants | products | $\Delta H_{0}$ | $\Delta H_{298}$ | $\exp ^{\text {a }}$ | $\frac{\Delta G_{298}}{\text { calc }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | calc | calc |  |  |
| $\mathrm{C}\left({ }^{3} \mathrm{P}\right)+\mathrm{CH}_{2} \mathrm{O}$ | T2 ( ${ }^{3} \mathrm{~A}^{\prime \prime}$ ) | -97.7 | -98.7 | $-101.2^{\text {b }}$ | -91.1 |
| $\mathrm{C}\left({ }^{1} \mathrm{D}\right)+\mathrm{CH}_{2} \mathrm{O}$ | $\mathbf{S 2}\left({ }^{1} \mathrm{~A}_{1}\right)$ | -179.0 | -180.1 | -184.1 | -171.7 |
| T2 ( ${ }^{3} \mathrm{~A}^{\prime \prime}$ ) | $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ | 20.7 | 22.3 | $24.5{ }^{\text {b }}$ | 12.9 |
| S2 ( ${ }^{1} \mathrm{~A}_{1}$ ) | $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ | 84.9 | 86.6 | 87.3 | 76.2 |
| S2 ( ${ }^{1} \mathrm{~A}_{1}$ ) | $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ | 105.4 | 107.1 | 112.2 | 97.0 |
| S2 ( ${ }^{1} \mathrm{~A}_{1}$ ) | $\mathrm{CO}+\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$ | 128.0 | 130.5 | 138.4 | 123.1 |
| $\mathrm{C}\left({ }^{3} \mathrm{P}\right)+\mathrm{CH}_{2} \mathrm{O}$ | $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{3} \mathrm{~B}_{1}\right)$ | -77.0 | -76.4 | -76.7 | -78.2 |
| $\mathrm{C}\left({ }^{1} \mathrm{D}\right)+\mathrm{CH}_{2} \mathrm{O}$ | $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~A}_{1}\right)$ | -94.1 | -93.5 | -96.8 | -95.5 |
| $\mathrm{C}\left({ }^{1} \mathrm{D}\right)+\mathrm{CH}_{2} \mathrm{O}$ | $\mathrm{CO}+\mathrm{CH}_{2}\left({ }^{1} \mathrm{~B}_{1}\right)$ | -73.6 | -73.0 | -72.9 | -75.1 |
| $\mathrm{C}\left({ }^{1} \mathrm{D}\right)+\mathrm{CH}_{2} \mathrm{O}$ | $\mathrm{CO}+\mathrm{CH}_{2}\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$ | -51.1 | -49.6 | -45.7 | -48.6 |

${ }^{a} \Delta H_{298}$ values are given. For detailed information about the experimental values, see Table 2. ${ }^{b} \mathbf{T} 2$ energies are calculated from a $\mathbf{S 2}\left({ }^{1} \mathrm{~A}_{1}\right)-\mathbf{T} 2\left({ }^{3} \mathrm{~A}^{\prime \prime}\right)$ separation of $54.8 \mathrm{kcal} / \mathrm{mol}$, reported by Schaefer in ref 18 b , with heat capacity corrections obtained in this study.
singlet ${ }^{1} B_{1}$ carbene producing the reaction is calculated to be $-75.1 \mathrm{kcal} / \mathrm{mol}$ (Table 5).

After a thorough examination of the $\mathrm{C}+\mathrm{CH}_{2} \mathrm{O}$ PES, we feel that singlet excited carbene generation is not a likely

[^8]Table 6. Relative Energies ( $\mathrm{kcal} / \mathrm{mol}$ ), Enthalpies ( $\mathrm{kcal} / \mathrm{mol}$ ) at 0 and 298 K , and Free Energies ( $\mathrm{kcal} / \mathrm{mol}$ ) at the PBE1PBE/
$6-311+G(2 d, p)$ Level of Species on the Ketene Plus (Z)-2-Butene Potential Energy Surface

|  | $\Delta E$ | $\Delta H_{0}$ | $\Delta H_{298 k}$ | $\Delta G_{298 \mathrm{~K}}$ |
| :---: | :---: | :---: | :---: | :---: |
| cis-butene + ketene | 0.0 | 0.0 | 0.0 | 0.0 |
| TS1 | 38.4 | 40.2 | 39.2 | 51.3 |
| cis 5ring | 14.7 | 19.9 | 18.1 | 32.0 |
| TS2 ${ }^{a}$ | 51.9 | 50.6 | 50.7 | 59.5 |
| cis-cyclopropane +CO | -9.6 | -7.6 | -8.0 | -6.2 |
| $\mathbf{T S 3}{ }^{a}$ | 36.5 | 37.4 | 36.8 | 47.4 |
| cis biradical ${ }^{a}$ | 27.6 | 29.7 | 29.1 | 39.9 |
| TS4 | 31.3 | 33.8 | 32.5 | 45.0 |
| trans biradical ${ }^{a}$ | 26.5 | 28.5 | 28.0 | 38.7 |
| $\mathbf{T S 5}^{a}$ | 30.8 | 33.1 | 31.8 | 44.4 |
| trans 5ring | 13.5 | 18.5 | 16.8 | 30.4 |
| TS6 $^{a}$ | 51.2 | 49.8 | 49.8 | 59.4 |
| trans-cyclopropane +CO | -10.9 | -9.0 | -9.4 | -7.1 |
| TS7 | 24.3 | 26.8 | 25.5 | 38.4 |
| cyclobutanone | -28.2 | -23.2 | -24.7 | -11.5 |
| TS8 ${ }^{a}$ | 31.1 | 32.8 | 31.8 | 43.4 |
| biradical ${ }^{a}$ | 29.7 | 31.7 | 31.1 | 41.7 |
| TS9 ${ }^{a}$ | 51.0 | 49.5 | 49.6 | 58.1 |

[^9]explanation for the experimental observation reported by Shevlin and co-workers. ${ }^{13}$ Hence, we explored the possibility that ( $Z$ )-2-butene could trap "hot" ketene. Ketene is known to react with $\pi$-bond systems. ${ }^{42}$ Therefore, it is possible that the ketene formed from the reaction of $C\left({ }^{1} \mathrm{D}\right)$ atom with formaldehyde can add to ( $Z$ )-2-butene and then undergo several steps of rearrangement to give the observed products, CO and cyclopropane. The reaction between ketene and ( $Z$ )-2-butene was studied by using
the same PBE1PBE density functional with a $6-311+G(2 d, p)$ basis set. Relative energies, enthalpies, and free energies are reported in Table 6, and a schematic potential energy surface for the reaction of ketene and $(Z)$-2-butene is given in Figure 7. Ketene can react with ( $Z$ )-2-butene in three ways: $[2+3]$ concerted addition to a $\pi$-bond, $\mathrm{C}-\mathrm{C}$ coupling addition followed by rotation around the $\mathrm{C}-\mathrm{C}$ bond, and $[2+2]$ cycloaddition. The $[2+3]$ concerted addition has the highest enthalpy barrier ( $39.2 \mathrm{kcal} / \mathrm{mol}$ ), and $\mathrm{C}-\mathrm{C}$ coupling addition is second highest ( $36.8 \mathrm{kcal} / \mathrm{mol}$ ). The lowest pathway is the well-known [2+2] cycloaddition ${ }^{42}(25.5 \mathrm{kcal} / \mathrm{mol})$, which will lead to a stable cyclobutanone. The $\mathrm{C}-\mathrm{C}$ coupling addition will lead to a cis biradical intermediate, which can isomerize to a trans biradical intermediate. Both biradical intermediates can undergo ring closure to yield cyclopropane and CO as products. More likely, ketene will follow the lowest enthalpy pathway to form cyclobutanone, which can undergo ring-opening to a biradical followed by release of CO to form trans-1,2-dimethylcyclopropane. In "room temperature" chemical reactions, cyclobutanone can be isolated. However, because ketene is formed from the reaction of $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ atom with $\mathrm{CH}_{2} \mathrm{O}, 170 \mathrm{kcal} / \mathrm{mol}$ extra energy is carried over. Thus, the new-born cyclobutanone is formed very hot, and the $\mathrm{C}-\mathrm{C}$ bond can be broken easily. The three pathways to the products are very competitive, since their enthalpic barrier heights are similar (50.7, 49.8, and $49.6 \mathrm{kcal} /$ mol ). If the ketene encounters ( $Z$ )-2-butene before relaxation, these high barriers can be overcome easily. Therefore, we suggest that this is the best explanation for the observed cis-


Figure 7. Potential energy surface for the reaction of ketene with ( $Z$ )-2-butene. The values in parentheses are enthalpies at 298 K in kilocalories per mole calculated at the PBE1PBE/6-311+G(2d,p) level.
and trans-1,2-dimethylcyclopropane formation in the C atom reaction with formaldehyde. We find it interesting that 25 years ago Dewar and co-workers proposed ${ }^{10}$ a similar mechanism of carbene formation via a ketene intermediate in the reaction of C atoms plus butanal.

## Conclusion

The reactions of triplet $\left({ }^{3} \mathrm{P}\right)$ and singlet $\left({ }^{1} \mathrm{D}\right)$ atomic carbon with formaldehyde were studied computationally. Ketene S2 $\left({ }^{1} \mathrm{~A}_{1}\right)$ is the global minimum on the $\mathrm{CH}_{2} \mathrm{CO}$ potential energy surface. On the triplet PES, a C atom adds to the $\mathrm{C}-\mathrm{O}$ double bond to form cyclic $\mathbf{T 1}$, which undergoes intramolecular rearrangement. The bent $\mathrm{H}_{2} \mathrm{C}-\mathrm{C}-\mathrm{O}$ linkage ketene isomer (T2) is lowest on the triplet PES, and it dissociates to give CO and the ground-state methylene $\left({ }^{3} \mathrm{~B}_{1}\right)$. On the triplet surface, linear $\mathrm{C}-\mathrm{C}-\mathrm{O}$ or $\mathrm{C}-\mathrm{O}-\mathrm{C}$ isomers ( $\mathbf{T 2 2}{ }^{\prime}$ and $\mathbf{T 5 5}$ ) were found to be transition states for the interconversion of corresponding bent isomers (T2 and T5). Hydrogen abstraction from formaldehyde by $\mathrm{C}\left({ }^{3} \mathrm{P}\right)$ is nonspontaneous ( $4.1 \mathrm{kcal} / \mathrm{mol}$ ) and can proceed without a reverse free energy barrier. On the singlet surface, the $\mathrm{C}\left({ }^{1} \mathrm{D}\right)$ addition to the $\mathrm{C}-\mathrm{O}$ double bond also occurs without barrier to form $\mathbf{S} 1$ with a free energy change of $-103.0 \mathrm{kcal} /$ mol. Intermediate $\mathbf{S} \mathbf{1}$ can also undergo various isomerization reactions to form the global minimum $\mathbf{S 2}$ or $\mathbf{S 5}$, which is the second lowest species on both potential energy surfaces. On both surfaces, intermediate carbenes are identified (T4 and S3).

Two possible pathways to form excited singlet methylene $\left({ }^{1} \mathrm{~B}_{1}\right)$ were found. One is along the reaction path $\operatorname{Sr} 7\left({ }^{1} \mathrm{~A}_{2}\right) \rightarrow$
$\mathbf{S 7}\left({ }^{1} \mathrm{~A}^{\prime \prime}\right) \rightarrow \mathbf{S 7} \mathbf{p}\left({ }^{1} \mathrm{~A}^{\prime \prime}\right)$, which leads to the ${ }^{1} \mathrm{~B}_{1}$ carbene directly, and the other is by way of $\mathbf{S \mathbf { 2 } ^ { \prime \prime }}$, which is the lowest-erergy species on the ${ }^{1} \mathrm{~A}^{\prime \prime}$ surface. Interestingly, the ground state $\mathbf{S} 2$ $\left({ }^{1} \mathrm{~A}_{1}\right)$ correlates with the third excited singlet state methylene $\left(\mathrm{c}^{1} \mathrm{~A}_{1}\right)$ rather than the first excited singlet methylene $\left({ }^{1} \mathrm{~A}_{1}\right)$. We also suggest that an alternative explanation of formation of cisand trans-1,2-dimethylcyclopropane by the reaction of energetic ketene with ( $Z$ )-2-butene. The ultimate answer to products of the $\mathrm{C}+\mathrm{CH}_{2}=\mathrm{O}$ reaction requires a consideration of the dynamic behavior. We are currently carrying out ab initio molecular dynamics calculations on the basis of our constructed potential energy surfaces.

Acknowledgment. Computer time was made available on the Auburn COSAM PRISM cluster and the Alabama Supercomputer center SGI Altix cluster.

Supporting Information Available: Table S1, Cartesian coordinates of all optimized structures obtained at the CASSCF$(14,13) / 6-311+G(2 d, p)$ level in Table 1; Table S2, the absolute energies (hartrees), zero-point energies ( $\mathrm{kcal} / \mathrm{mol}$ ), heat capacity corrections to $298 \mathrm{~K}(\mathrm{kcal} / \mathrm{mol})$, entropies ( $\mathrm{cal} / \mathrm{mol} \cdot \mathrm{K}$ ), and spinsquared values at the PBE1PBE/6-311+G(2d,p) level for the species in Table 6; the full citation to ref 24 is given. This material is available free of charge via the Internet at http://pubs.acs.org.

JA060216M


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